

To \_\_\_\_\_

Date 6-28-90

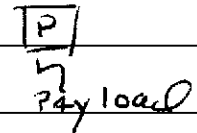
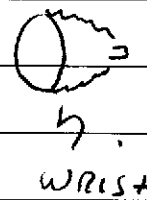
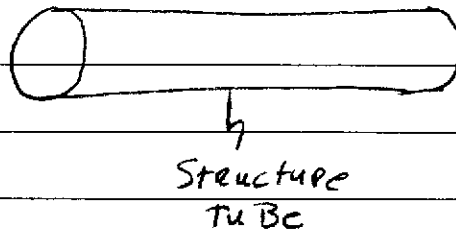
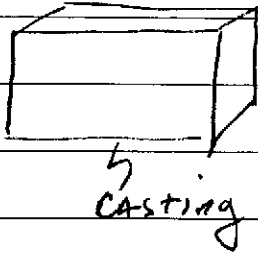
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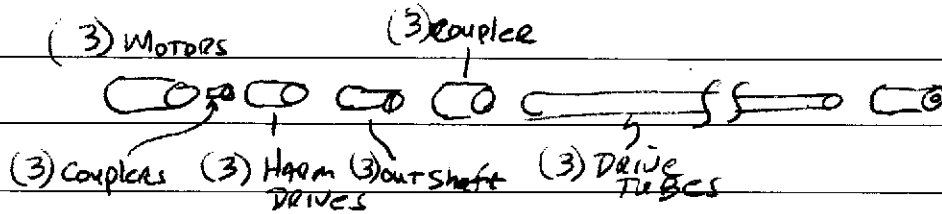
Subject Horiz Arm Calculations

Components - External

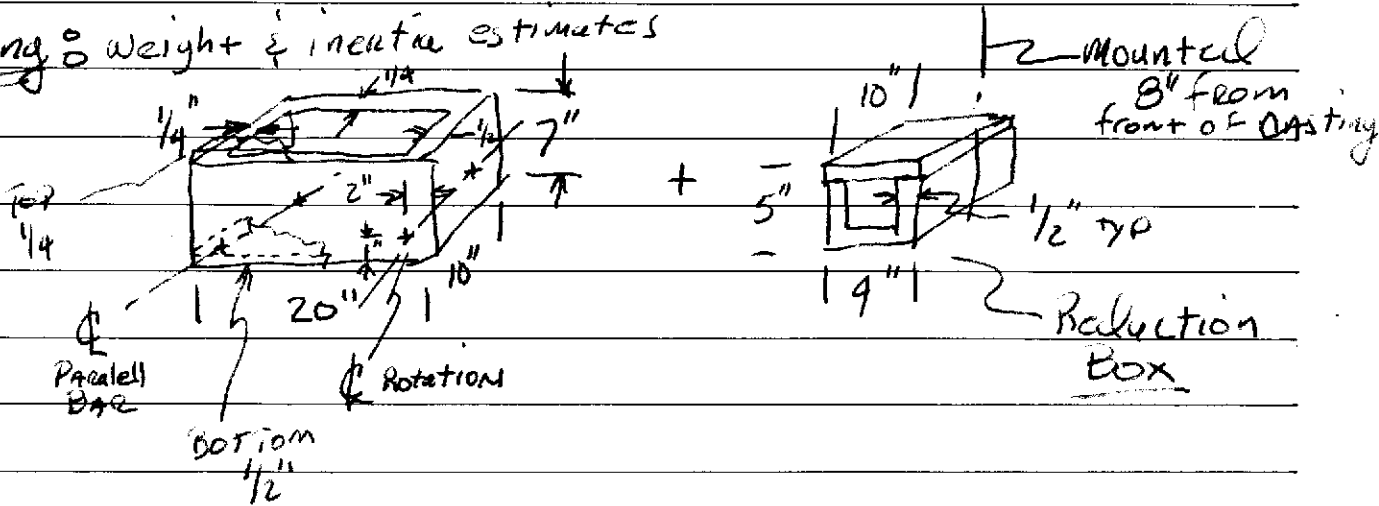
$\alpha_{ST} = .283 \text{ lb/in}^3$   
 $\alpha_{AI} = .099$



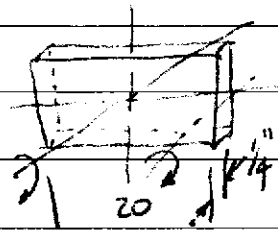
Components - Internal



Casting Weight & inertia estimates



(2) Sides



$J_{rot} = \frac{m(20^2 + 7^2)}{12} =$   
 $J_{trans} = 8.38^2 \cdot m$

18"

$m = 7 \times 20 \times .25 \times .099 \text{ lb/in}^3 = 3.465 \text{ lb}$

$J_{side} = m(8.38^2 + 37.42) = m \cdot 107.64 \text{ in}^2$   
 $J_{side-total} = 2(m \cdot 107.64) = m \cdot 42.28 \text{ in}^2$

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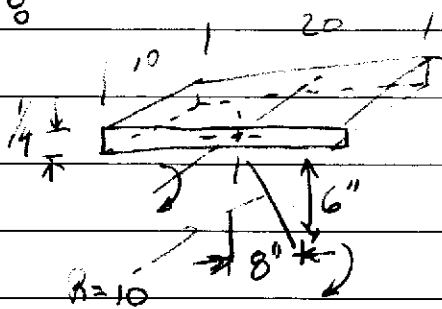
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Subject Horiz Arm Calculations

Top



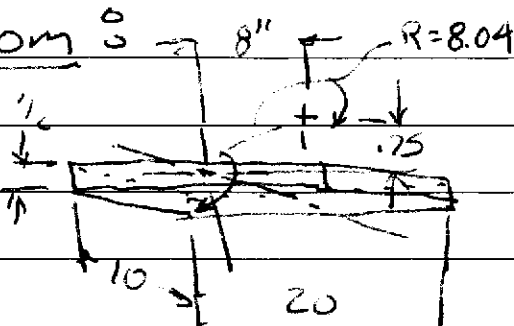
$$W = 10 \times 20 \times .25 \times 0.099 = 4.95 \text{ lbf}$$

$$J_{\text{TRANS}} = (10'')^2 m = 100 m$$

$$J_{\text{ROT}} = \frac{m (.25^2 + 20^2)}{12}$$

$$\therefore J_{\text{TOT}} = m \cdot 33.34 \text{ in}^2 \quad // \quad J_{\text{TOT}} = 133.34 m$$

Bottom



$$J_{\text{TRANS}} = m \cdot 64.56 \text{ in}^2$$

$$J_{\text{ROT}} = \frac{m (10^2 + 20^2)}{12}$$

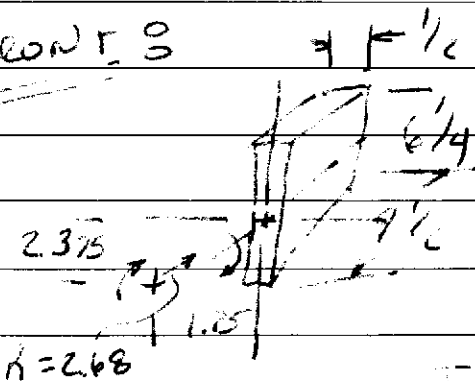
$$\therefore J_{\text{TOT}} = m \cdot 33.354$$

$$J_{\text{BOTTOM}} = m \cdot (64.56 + 33.354)$$

$$\therefore J_{\text{BOTTOM}} = m \cdot 97.91 \text{ in}^2$$

$$[W = 10 \cdot 20 \cdot 0.5 \cdot 0.099 = 9.9 \text{ lbf}]$$

Front



$$W = 4.5 \cdot 6.25 \cdot 0.5 \cdot 0.099 = 2.94 \text{ lbf}$$

$$J_{\text{TRANS}} = m \cdot (2.68 \text{ in})^2 = m \cdot 7.18$$

$$J_{\text{ROT}} = \frac{m (.5^2 + 6.25^2)}{12}$$

$$J_{\text{TOT}} = m \cdot 3.28 \text{ in}^2$$

$$J_{\text{FRONT}} = m (7.18 + 3.28) = m \cdot 10.46 \text{ in}^2$$

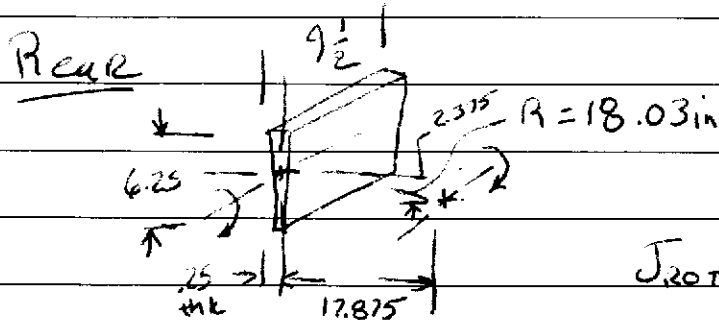
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Subject Horiz Arm Calculations



$$W = 6.25 \times 9.5 \times 2.5 = 0.099$$

$$= 1.47 \text{ lbs}$$

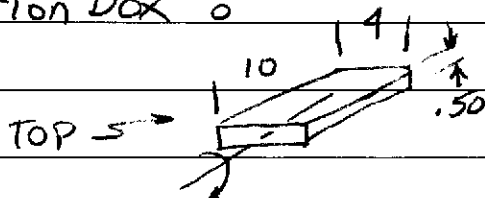
$$J_{\text{TRANS}} = m (18.03)^2 = m \cdot 325.08 \text{ in}^2$$

$$J_{\text{ROT}} = m (.25^2 + 6.25^2) / 12$$

$$= m \cdot 3.26 \text{ in}^2$$

$$J_{\text{Rear}} = m (325.08 + 3.26) = m \cdot 328.34 \text{ in}^2$$

Reduction Box

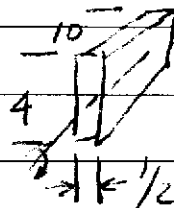


$$W = 10 \cdot 4 \cdot .50 \cdot 0.099 = 1.98 \#$$

$$J_{\text{ROT}} = m \cdot (.50^2 + 4^2) / 12$$

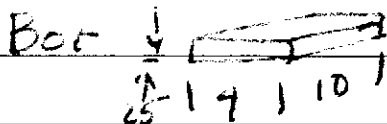
$$= m \cdot 1.35 \text{ in}^2$$

(2) sides



$$W = 4 \cdot 10 \cdot .50 \cdot 0.099 = 1.98 \#$$

$$J_{\text{ROT}} = m \cdot 1.35 \text{ in}^2$$

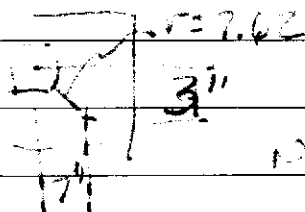


$$W = 1.98$$

$$J_{\text{ROT}} = m \cdot 1.35 \text{ in}^2$$

$$J_{\text{ROT of Box}} = 4 (m \cdot 1.35 \text{ in}^2) = m \cdot 5.4$$

$$J_{\text{Translation}} = m \cdot r^2 = m \cdot 3.62^2 = m \cdot 58 \text{ in}^2 \text{ } \leftarrow \text{Assumes Point Load.}$$



$$J_{\text{Box Total}} = m (5.4 + 58) = m \cdot 63.4 \text{ in}^2$$

$$100 \# = 3 W_{\text{Box}} = 4 \cdot 1.98 = 7.92$$

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TOTAL Casting Inertia - (Less internal components)

$$\begin{aligned}
 J_{\text{Total}} &= 2 J_{\text{side}} + J_{\text{TOP}} + J_{\text{BOT}} + J_{\text{Front}} + J_{\text{rear}} + J_{\text{radix}} \\
 &= 2(3.465 \text{ lb}_f \cdot 107.64 \text{ in}^2) + (133.34 \text{ in}^2 \cdot 4.75 \text{ lb}_f) + (9.9 \text{ lb}_f \cdot 97.9 \text{ in}^2) \\
 &\quad + (2.94 \text{ lb}_f \cdot 10.46 \text{ in}^2) + (1.47 \text{ lb}_f \cdot 328.34) + (7.92 \text{ lb}_f \cdot 63.4 \text{ in}^2) \\
 &= 745.95 \text{ lb}_f \text{ in}^2 + 660.03 \text{ lb}_f \text{ in}^2 + 969.21 \text{ lb}_f \text{ in}^2 \\
 &\quad + 30.75 \text{ lb}_f \text{ in}^2 + 482.99 + 502.13 \\
 &= \underline{3,391.06 \text{ lb}_f \text{ in}^2}
 \end{aligned}$$

$$(\text{lb}_f \text{ in}^2) \left( \frac{f \cdot t^2}{144 \text{ in}^2} \right) \left( \frac{\text{slug}}{32.17 \text{ lb}_f} \right) \left( 0.3731 \frac{\text{in lb sec}^2}{\text{lb}_f f \cdot t^2} \right) (32.17)$$

$$\text{lb}_f \text{ in}^2 \times \frac{.3731}{144} = \text{in lb sec}^2$$

conversion

$$\text{Factor } 2.591 \times 10^{-3} \cdot \text{lb}_f \text{ in}^2 = \text{in lb sec}^2$$

$$\therefore J_{\text{Total Casting}} = (3,391.06 \text{ lb}_f \text{ in}^2) (2.591 \times 10^{-3}) = 8.786 \text{ in lb sec}^2$$

$$J_{\text{Total Casting}} = 8.786 \text{ in lb sec}^2$$

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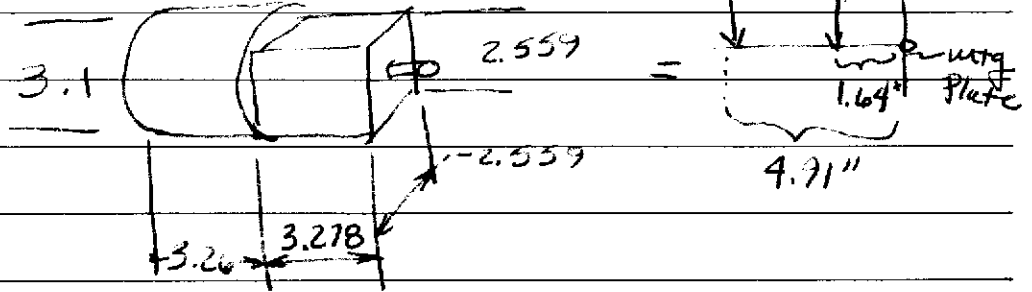
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Subject Horizontal Arm Calculations

Casting - Internal Components.

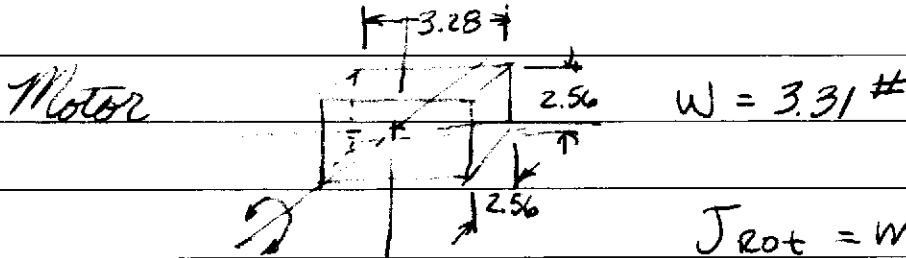
(3) Motors



$W_{\text{motor}} = 3.3 \text{ lbs}$

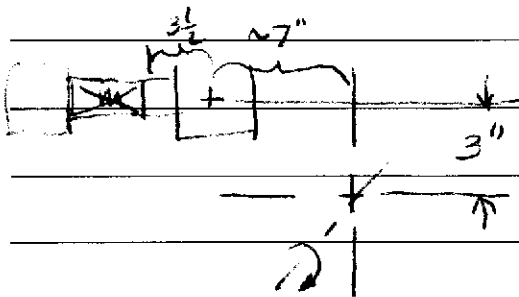
$W_{m+E} = 4.41 \text{ lbs}$

$\therefore W_E = 1.11 \text{ lbs}$



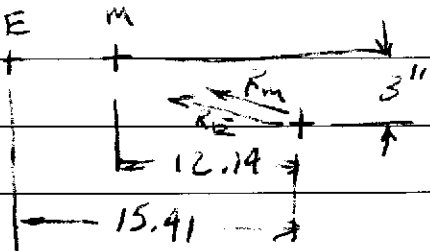
$J_{\text{rot}} = m(2.56^2 + 3.28^2) / 12$   
 $= m \cdot 1.443 \text{ in}^2$

$J_{\text{trans}} = m \cdot (12.51 \text{ in})^2$   
 $= m \cdot 156.50 \text{ in}^2$



Encoder  $J_{\text{rot}} = \frac{m(3r^2 + l^2)}{12}$   
 $= \frac{m(3 \cdot 7.21^2 + 10.63)}{12}$

$\therefore J_{\text{rot}} = m \cdot 1.486 \text{ in}^2$   
 $J_{\text{trans}} = m \cdot 237.47 \text{ in}^2$



$R_{mE} = 12.51$

$R_{E} = 15.70$

$J_{m+E} = 3.31(1.443 + 156.5) + 1.11(1.486 + 237.47)$   
 $= 788.03 \text{ in}^2 \text{ lbs} = (2.571 \times 10^{-3})$   
 $= 2.042 \text{ in lbs sec}^2$

$J_{\text{motors \& encoder}} = 6.125 \text{ in lbs sec}^2$

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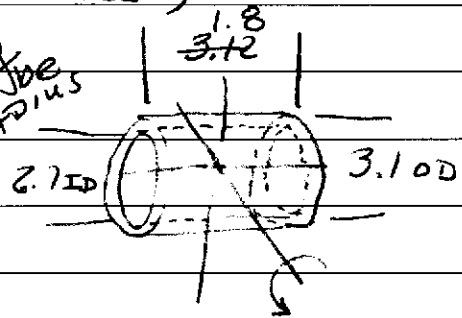
Subject Horizontal Item Calculations

Casting internal components. (cont'd)

Motor Mount Adapter

$$W = 1.8 \times 0.099 \times \pi \times (3.1^2 - 2.7^2)$$

$$= 1.30 \#$$



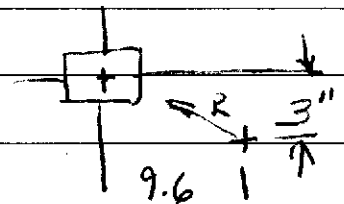
$$J_{rot} = m \left( 3 \cdot \left( \frac{2.7}{2} \right)^2 + 3 \left( \frac{3.1}{2} \right)^2 + (1.8)^2 \right) / 12$$

$$= m (5.4675 + 7.2075 + 3.24) / 12$$

$$m \cdot 1.326 \text{ in}^2 = m \cdot 0.3315$$

$$J_{TRANS} = m (10.06)^2 = 101.16 m \text{ in}^2$$

~~25.29 m~~

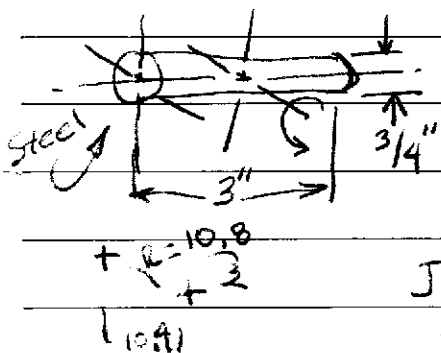


$$J_{mm \text{ Adapter}} = (3) (101.16 + 1.326) (2.591 \times 10^{-3})$$

$$r = 10.06''$$

$$J_{mm \text{ Adapter}} = 0.7966 \text{ in lb sec}^2$$

Shaft Adapter to H. D. Wave Generator



$$W = 3 \cdot \left( \frac{.75}{2} \right)^2 \cdot \pi \cdot 0.099 = 0.04375 \text{ lbf}$$

$$J_{rot} = m (3 (.375)^2 + 9) / 12 = .785 m \text{ in}^2$$

$$J_{TRANS} = m \cdot 116.95 \text{ in}^2$$

$$J_{TOTAL} = (3) (.375) (116.95) (2.591 \times 10^{-3}) = .341 \text{ in lb sec}^2$$

$$J_{shaft \text{ adapter total}} = 0.341 \text{ in lb sec}^2$$

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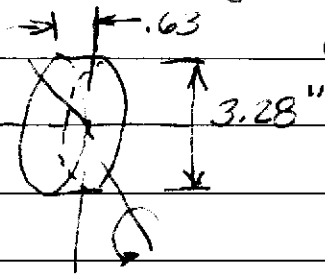
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Subject Horiz. Arm Calculations

Casting internal components (contd.)

③ Harmonic Drives E-HD 5C - Bulk or weight is in the wave gen & Circular Spline - can approx geometry

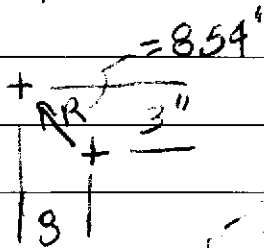


Weight = 1.2 lb

$$J_{rot} = \frac{mr^2}{4} = m \left(\frac{3.28}{2}\right)^2 / 4 = 1.2 \times .674$$

$$= (.807 \text{ lb} \cdot \text{in}^2) (2.591 \times 10^{-3})$$

$$= 2.091 \times 10^{-3} \text{ in} \cdot \text{lb} \cdot \text{sec}^2$$



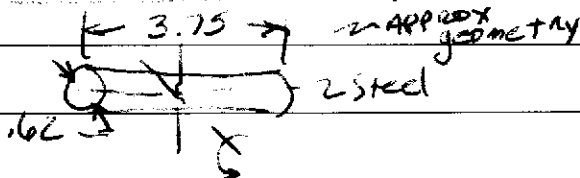
$$J_{trans} = mr^2 = 1.2 \times (8.54^2) = 2.591 \times 10^{-3}$$

$$= 0.227 \text{ in} \cdot \text{lb} \cdot \text{sec}^2$$

$$J_{TOTAL} = (3) (2.091 \times 10^{-3} + 0.227)$$

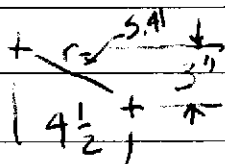
$$= 0.687 \text{ in} \cdot \text{lb} \cdot \text{sec}^2$$

Harmonic Drive Output Shaft 3



$$\text{Weight} = \pi \cdot .283 \cdot 3.75 \cdot (.31)^2$$

$$= 0.320 \text{ lb}$$



$$J_{rot} = m (3 \cdot (.31)^2 + 3.75^2) / 12$$

$$= 0.320 \cdot (1.194) (2.591 \times 10^{-3})$$

$$= 9.915 \times 10^{-4} \text{ in} \cdot \text{lb} \cdot \text{sec}^2$$

$$J_{trans} = 0.320 \times 5.41^2 \times 2.591 \times 10^{-3} = 2.427 \times 10^{-2} \text{ in} \cdot \text{lb} \cdot \text{sec}^2$$

$$J_{TOTAL \text{ shaft}} = 2.526 \times 10^{-2} \text{ in} \cdot \text{lb} \cdot \text{sec}^2$$

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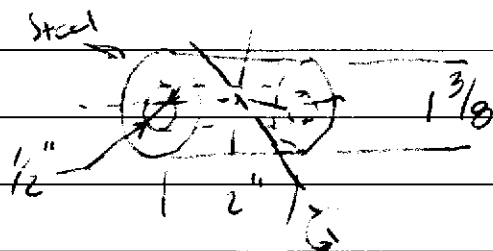
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Subject Horiz Arm Calculations

Casting Internal Components (contd.)

H.O.D. Output Shaft + Coupler



$$M = \pi \cdot 283 \cdot 2 \cdot \left( \left( \frac{1.375}{2} \right)^2 - (25)^2 \right)$$

$$= 0.729 \text{ lb}_f$$

$$J_{rot} = 0.729 (3(25^2) + 3(16875) + 4) / 2$$

$$= (-.341) (2.591 \times 10^{-3}) = 8.823 \times 10^{-4} \text{ in}^4 \text{ lb}_f \text{ sec}^2$$

$$J_{trans} = 0.729 \cdot 9 \cdot 2.591 \times 10^{-3}$$

$$= 1.7 \times 10^{-2} \text{ in} \text{ lb}_f \text{ sec}^2$$

$$J_{coupler \text{ total}} = 3 \cdot (1.7 \times 10^{-2} + 8.823 \times 10^{-4})$$

$$= 5.365 \times 10^{-2} \text{ in} \text{ lb}_f \text{ sec}^2$$

Total Casting Internal Components.

$$J_{internal} = J_{MTE} + J_{MMA} + J_{SA} + J_{HD} + J_{HROS} + J_{coupler}$$

$$= 6.125 + 0.7966 + 0.341 + 0.687 + 2.526 \times 10^{-2} + 5.365 \times 10^{-2}$$

$$= 8.029 \text{ in} \text{ lb}_f \text{ sec}^2$$

$$J_{internal \text{ Component}} = 8.029 \text{ in} \text{ lb}_f \text{ sec}^2$$



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Subject Horiz Arm Calculations

Total Casting & Internal Components Inertia

$$J_e = J_{cast} + J_{ic} = 8.786 + 8.029 \text{ in lb sec}^2$$

$$J_e = 16.815 \text{ in lb. Sec}^2$$

Casting Moment Calculations

+ \*

Sides	(2)(8")(3.465 lbs)	= 55.44	in lbs.
Top	<del>(2)</del> (9")(4.95 lbs)	= 39.6	
Bottom	(3)(9.9#)	= 79.2	
Front	(-1.15")(2.94#)	= -5.145	
Rear	(18.795")(1.47#)	= 27.614	
Red Box	(7")(7.92 lbs)	= 55.44	~
Motor	(3)(12.14")(3.31 lbs)	= 120.186	in lbs
Encoder	(3)(15.41")(1.11 lbs)	= 51.315	
Motor Mnt Adapt	(3)(9.6)(1.3#)	= 37.44	
Shaft Adapter	(3)(10.41)(.375#)	= 11.71	
Worm Drive	(3)(8")(1.2#)	= 28.8	
H.V. cut shaft	(3)(9.5")(1.2#)	= 4.32	
H.D. cut shaft Adapter	φ		

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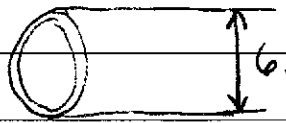
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Subject Hoiz Arm Calculations

Total Casting Moment = 505.92 in.lbs.

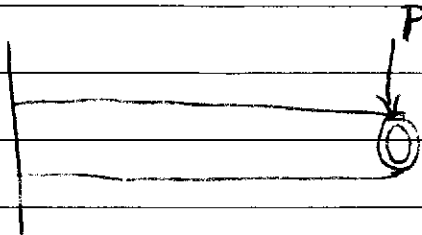
6061-T6



.125 wall - 2.713 #/ft

.188 wall - 3.996 #/ft

=

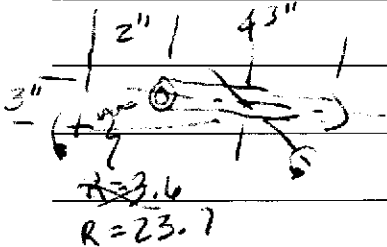


~~E<sub>6</sub>~~  
Mod of cast =  $10 \times 10^{10} \text{ lb/in}^2$

estimate P at  $P_{\text{load}} + P_{\text{weight}} + \text{Weight of arm/L} +$   
 $\text{Weight of drive tubes}$

Drive Tubes

43" long - 1" od x .884 ID steel



$$W = 43 \times .283 \times \pi \left( \frac{1^2}{4} - \frac{.884^2}{4} \right) = 2.09 \text{ lbs.}$$

$$J_{\text{tot}} = \pi \left( \frac{1^4}{64} + 3 \left( \frac{.442^4}{64} + 43^2 \right) \right) / 12 = (322.27) (2.591 \times 10^{-3}) = 0.835 \text{ in}^4 \text{ lb sec}^2$$

Total

$$J_{\text{tubes}} = 2.89 \text{ in}^4 \text{ lb sec}^2$$

$$J_{\text{arms}} = m r^2 = 2.09 \cdot 13 \cdot (2.591 \times 10^{-3}) = (2.09 \#) (23.7)^2 = (49.51) (2.591 \times 10^{-3}) = .128 \text{ in}^4 \text{ lb sec}^2$$

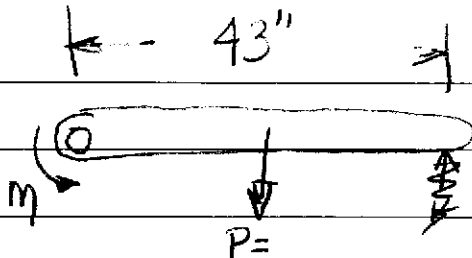
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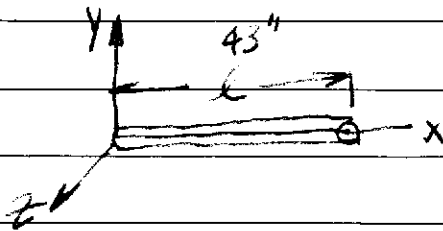
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Subject Howie Arm Calculations



Static moment  
 $= 2.09 \# \cdot \frac{43''}{2}$   
 $M_s = 44.94 \# \text{ in lbs.}$

Slender rod



$$I_y = \int x^2 dm = \int_0^L x^2 \frac{m}{L} dx = \left[ \frac{m}{L} \frac{x^3}{3} \right]_0^L$$

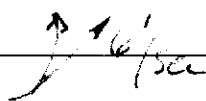
$$= \frac{mL^2}{3} = \frac{m(43)^2}{3} = 209 \text{ lbs} \cdot 43^2 / 3$$

$$= 406.67 \cdot 1288.14 (2.591 \times 10^{-3})$$

$$= 3.337 \text{ in lb sec}^2$$

TOTAL Arm length from pivot to tool post = ~62"

WANT  $\omega$  / second in 0.350 seconds



$$2\pi R = \pi D = \text{circ of Axis path}$$

$$= \pi \cdot 10.3 \text{ ft} = 32.5 \text{ ft}$$

@ 6 ft/sec tip speed

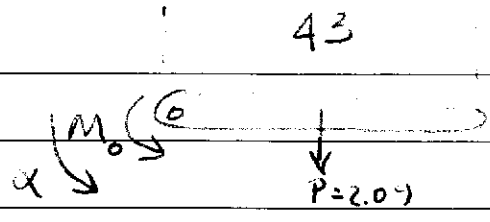
$$\omega = \frac{6/32.5 \text{ (ft/sec) / (ft/rev)}}{0.350} = 0.1848 \text{ rev/sec} \cdot 2\pi \text{ RAD/rev}$$

$$= 1.1613 \text{ RAD/sec}$$

$$\alpha = \frac{\omega}{t} = \frac{1.1613}{.350} = 3.318 \text{ RAD/sec}^2$$

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$$\sum M = (-2.07) \left( \frac{43}{2} \right) + M_o = \bar{I} \alpha$$

$$\therefore M_o = \bar{I} \alpha + 44.935 \text{ in lbs}$$

$$= (3.337 \text{ in lb sec}^2) (3.318 \text{ RAD/sec}^2) + 44.935 \text{ in lb}$$

$\therefore M_o = 56 \text{ in lbs}$  torque reqd to ~~move~~ ROTATE one drive tube at reqd accel.

Total force at the end of tube to accel 3 drive tubes =  $3 (56 \text{ in lbs}) = (168 \text{ in lbs} \div 43") = 3.91 \text{ lbs}$

Total force for the structure tube (assuming slender rod) weight  $4' \times 2.7 \#/\text{ft} = 10.8 \text{ lbs}$

$$J = \frac{m l^2}{3} = \frac{10.8 \cdot (48)^2}{3} (2.951 \times 10^{-3}) = 24.48 \text{ in lb sec}^2$$

$$\sum M_o = -24.48 \cdot 48 + M_o = 24.48 \cdot 3.318 \text{ sec}^2$$

$$\therefore M_o = 10.8 \cdot 48 + (24.48 \text{ in lb sec}^2) (3.318 \text{ sec}^2) = 518.4 + 81.22 = 600 \text{ in lbs.}$$

equiv Force @ END =  $600 / 48 = 12.5 \text{ lbs}$

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$\frac{M}{A} = F^2$   
Payload @ Wrist = 25#

$$\sum M = I \alpha = M - (25\# \cdot 48") = 25 \cdot (48)^2 \cdot 2.591 \times 10^{-3}$$

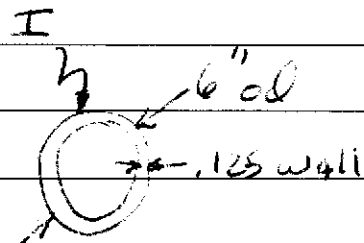
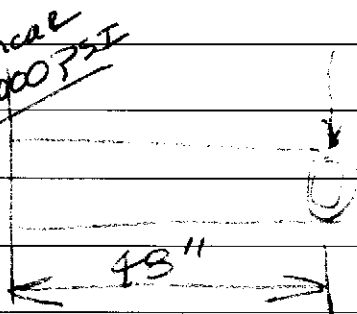
$$\therefore M = 1200 + 149.24 = 1350 \text{ in lb}$$

$$\therefore \text{equiv Force @ end} = 1350/48 = \underline{112.4 \text{ lbs}}$$

TOTAL forces in this model for deflection & STRESS estimates

$$F = 3.91 + 12.5 + 112.4 = 128.41 \#$$

Notes  
Ultimate Shear  
Strength = 30,000 PSI



for thin wall tubes

$$\tau = \frac{T}{2 A t} = \frac{128.41 \cdot 48"}{(2) \left(\frac{5.875}{2}\right) (0.125)}$$

thickness

$$I_0 = \pi R_{avg}^3 \cdot t$$

$$= \pi \left(\frac{5.875}{2}\right)^3 \cdot 0.125$$

$$= 9.954 \text{ in}^4$$

$$\text{deflection} = \frac{W l^3}{E I} = \frac{(128.41)(48^3)}{(10.0 \times 10^6)(9.958)}$$

$$= \underline{0.1426 \text{ inches}}$$

$$I = \frac{\pi}{64} (D_o^4 - d_i^4)$$

$$= \frac{\pi}{64} (6^4 - 5.75^4) \cdot 9.958 \text{ in}^4$$

$$\sigma = \frac{M y}{I} = \frac{5827.68 \cdot 6 \text{ in}}{9.958 \text{ in}^4}$$

$$\sigma = \underline{3511.4 \text{ PSI}}$$

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Subject Horizontal Arm Calc.

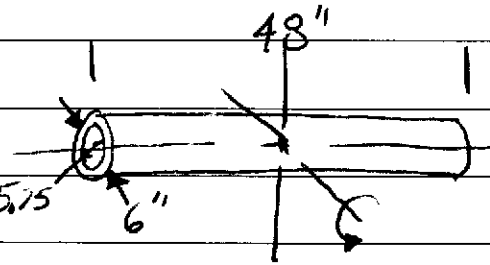
▣ Total Horiz Arm ▣

Loaded Casting:  $T_c = 505.92 \text{ in lb sec}^2$   
 $J_c = 16.815 \text{ in lb sec}^2$

Structure Tube

$W = 10.8 \text{ lb}$

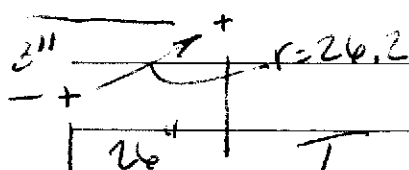
$J_{rot} = \frac{m}{12} (3 \left(\frac{5.75}{2}\right)^2 + 3(3^2 + 48^2))$



$J_{rot} = \frac{10.8}{12} (2355.8) (2.591 \times 10^{-3}) = 5.49 \text{ in lb sec}^2$

$J_{trans} = 10.8 \cdot (26.2)^2 \cdot (2.591 \times 10^{-3}) = 19.17 \text{ in lb sec}^2$

$J_{ST} = 24.66 \text{ in lb sec}^2$



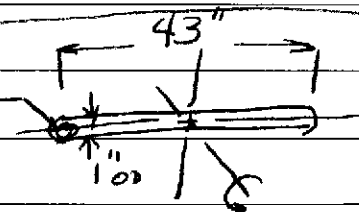
Torque =  $10.8 \cdot 26 = 280.8 \text{ in lb}$

Drive Tubes

$J_{rot} = 0.835 \text{ in lb sec}^2$

$J_{trans} = 0.1283 \text{ in lb sec}^2$

$J_{dr. total} = (3)(.835 + .1283) = 2.890 \text{ in lb sec}^2$



$\frac{2.890}{3} = 23.7$

Torque =  $(23.7)(3)(2.09\#) = 148.6 \text{ in lbs}$

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Subject Horiz Arm Calculations

Wrist Couplers (3)

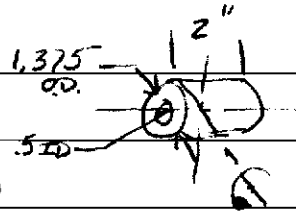
$$J_{rot} = 8.823 \times 10^{-4} \text{ in lb sec}^2$$

$$J_{trans} = (0.729\#)(47^2)(2.591 \times 10^{-3})$$

$$= 4.172 \text{ in lb sec}^2$$

$$J_{TOTAL} = (3)(8.823 \times 10^{-4} + 4.172) = 12.544 \text{ in lb sec}^2$$

$$Torque = (3)(0.729\#)(47") = 102.8 \text{ in lbs.}$$



Wrist (3)  $w = 12\#$   
 $r = 54"$

$$J = (12\#)(54\text{in})^2(2.591 \times 10^{-3})$$

$$= 90.66 \text{ in lb sec}^2$$

$$T = 12\# \cdot 54" = 648 \text{ in lb.}$$

Payload (3)  $w = 15\#$   
 $r = 66"$

$$J = (15\#)(66)^2(2.591 \times 10^{-3})$$

$$= 169.3 \text{ in lb sec}^2$$

$$T = 15 \cdot 66 = 990 \text{ in lb.}$$

Horiz Arm Totals

Casting  $J = 16.815$

$T = 505.92$

Struct. Tube  $J = 24.66$

$T = 280.8$

Wrist Tube  $J = 2.840$

$T = 148.6$

Couplers  $J = 12.544$

$T = 102.8$

wrist  $J = 90.66$

$T = 648 \text{ in lb.}$

Payload  $J = 169.3 \text{ in lb sec}^2$   $T = 990 \text{ in lb.}$

TOTAL  $J = 316.87 \text{ in lb sec}^2$   $T_{TOT} = 1664.28 \text{ in lbs}$   
 $= 138.69 \text{ ft-lbs.}$

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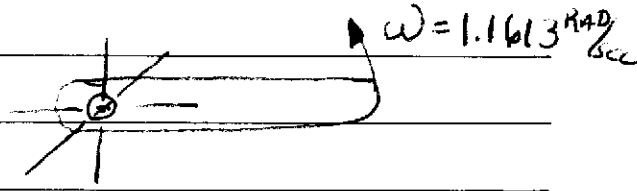
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Subject Horiz Arm Calculations

6 ft/sec Tip Speed

$$\omega = 0.1848 \text{ REV/SEC} = 1.1613 \text{ RAD/SEC}$$



$$J_{\text{hor arm}} = 316.87 \text{ in lb sec}^2$$

$$I_{\text{static}} = 1664.28 \text{ in lb}$$

Find GEAR Reduction BASED ON 6ft/second and an input of 3000 RPM

$$\omega_{\text{in}} = 3000 \left( \frac{\text{REV}}{\text{min}} \right) \left( \frac{\text{min}}{60 \text{ SEC}} \right) = 50 \text{ REV/SEC}$$

$$\omega_{\text{out}} = 0.1848 \text{ REV/SEC}$$

$$N = \frac{50}{0.1848} = 270.5627706 \approx 1$$

Use 2003A Harmonic Drive

φ8 YASKAWA

$$T_{\text{inst}} = 65 \text{ in lb} \quad J_m = 2.53 \times 10^{-3} \text{ in lb sec}^2$$

$$T_{\text{cont}} = 30 \text{ in lb}$$

Actual output TORQUE MAX = (200)(65 in lb) = 13,000 in lb.

Overestimated. using Peak torque

using cont torque outp. = (200)(.8)(30) =

USE BM FOR ~~Calc~~ Inertia ( $J_{\text{gm}} = 14.758 \text{ lb in}^2$ )

$$J_{\text{gm}} = 57.167 \text{ lb in}^2 = 0.1481 \text{ in lb sec}^2$$

386.15 Reflected system inertia =  $\frac{316.87}{(200)^2} = 7.922 \times 10^{-3} \text{ in lb sec}^2$

using BM  $R_i = \frac{7.922 \times 10^{-3} + 0.1481}{2.53 \times 10^{-3}} = 61.7$



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HARMONIC Drive Inertia			MOTOR Inertia	
Size	J (inlbsec <sup>2</sup> )	T <sub>max</sub>	Size	J (inlbsec <sup>2</sup> )
3C	$1.502 \times 10^{-4}$	470 @ 50:1	φ2	$1.1 \times 10^{-4}$
5C	$4.274 \times 10^{-4}$	530 @ 60:1	φ3	$4.5 \times 10^{-4}$
1M	$1.580 \times 10^{-3}$	4000 @ 200:1	φ5	$6.7 \times 10^{-4}$
2M	$4.533 \times 10^{-3}$	6600 @ 200:1	φ8	$2.53 \times 10^{-3}$
4M	$1.311 \times 10^{-2}$	15500 @ 200:1	15	$2.88 \times 10^{-3}$
8M	$5.077 \times 10^{-2}$	29,000 @ 200:1	3φ	$5.09 \times 10^{-3}$
15M	0.1334	50,000 @ 200:1		

use 4M HD with 08 motor  $T_{out} = 30 \cdot 200 \cdot 8 = 4800$

$$N_J = \frac{J_{inertial}}{J_m} = \frac{2.53 \times 10^{-3}}{2.53 \times 10^{-3}} = \frac{1.311 \times 10^{-2} + (316.87 / (2.53 \times 10^{-3}))}{2.53 \times 10^{-3}}$$

$$= 8.3$$

use 4M with 15 motor  $T_{out} = 55 \cdot 200 \cdot 0.8 = 8800$

$$N_J = \frac{J_L}{J_m} = \frac{2.103 \times 10^{-2}}{2.88 \times 10^{-3}} = 7.302$$

use 2M with 08 motor  $T_{out} = 4800$

$$N_J = \frac{J_L}{J_m} = \frac{4.533 \times 10^{-3} + 7.922 \times 10^{-3}}{2.53 \times 10^{-3}} = 4.92$$